

A new method for decoding phase codes

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Outline

- ▶ Recording the amplitude data
- ▶ Short introduction to lag profile inversion
- ▶ Comparison to alternating code decoding
- ▶ First results of a code pair experiment

Data recording

- ▶ The attenuated transmitter signals and ionospheric echoes are recorded in amplitude domain
- ▶ The digitizer is connected to the second IF stage of the radars
- ▶ Sampling frequency usually 1 MHz
- ▶ Raw samples saved in hard disk for later analysis

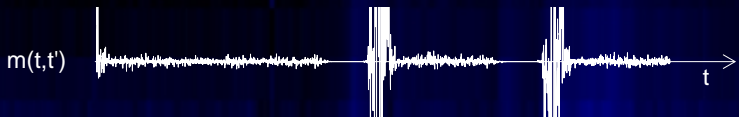
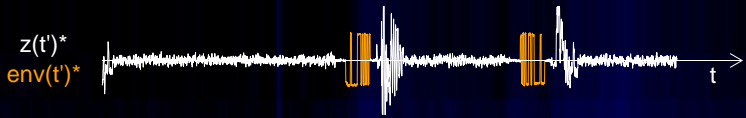
Lagged products and range ambiguity functions

- ▶ Transmission envelopes $env(t)$ and the echoes $z(t)$ in the same data stream
- ▶ A data vector contains one integration period of data
- ▶ Lagged products of the data vector and its complex conjugate
 - ▶ Ambiguous lagged products from the echo part

$$m_{\tau}(t) = z(t)\overline{z(t - \tau)}$$

- ▶ Range ambiguity functions from the transmission part

$$W_{\tau}(t, S) = env(t - S)\overline{env(t - \tau - S)}$$

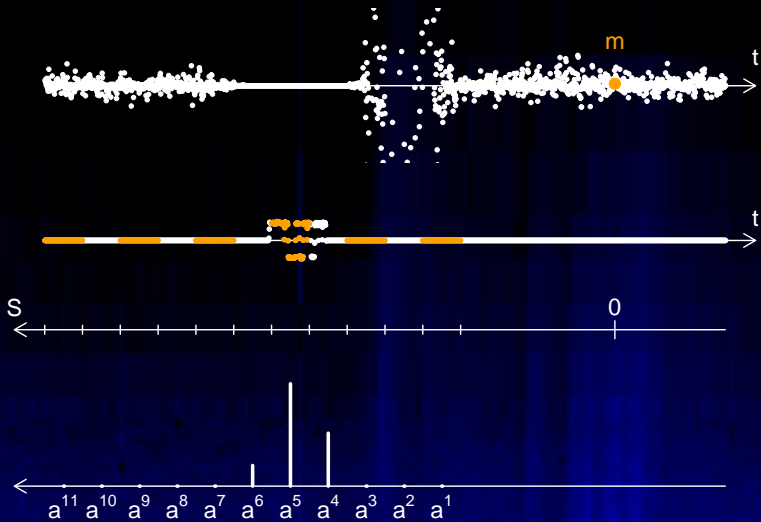


Lag profile inversion

- ▶ The radar beam is divided into range gates
- ▶ x_T^k is the unknown lag value in gate k
- ▶ Each $m_T(t)$ is a weighted sum of the unknowns x_T^k

$$m_T(t) = \sum_{k=1}^N a_T^k(t) x_T^k + \varepsilon_T(t),$$

- ▶ Coefficient $a_T^k(t)$ is the integral of $W_T(t, S)$ over range gate k



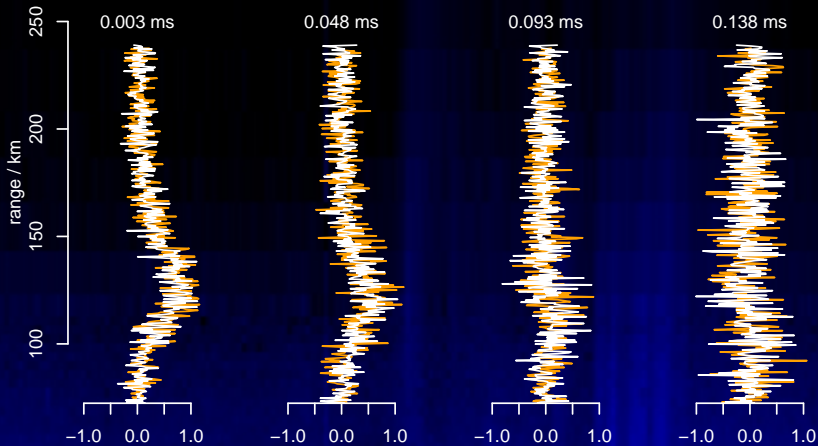
$$m = a^1 x^1 + a^2 x^2 + \dots + a^N x^N$$

- ▶ All lagged products from one integration period are collected in a large set of linear equations

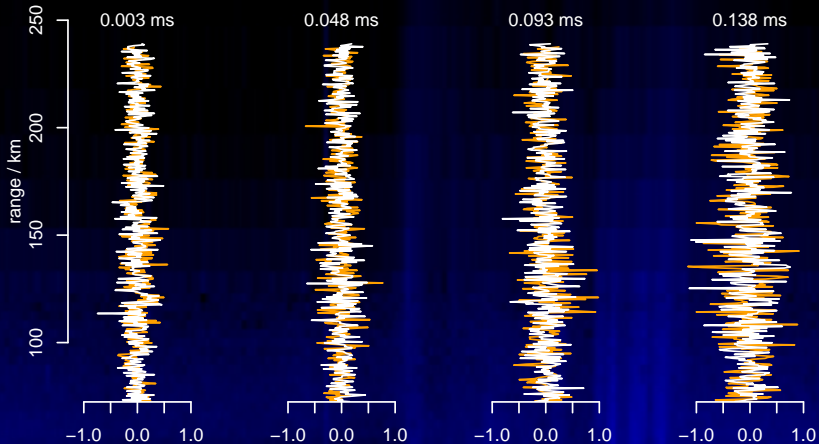
$$\mathbf{m}_T = \mathbf{A}_T \mathbf{x}_T + \boldsymbol{\varepsilon}_T$$

- ▶ The most probable lag profile and its variance can be solved with FLIPS
- ▶ The same procedure for all lag profiles \Rightarrow ACF
- ▶ Parameter fit to the ACF using iterative methods

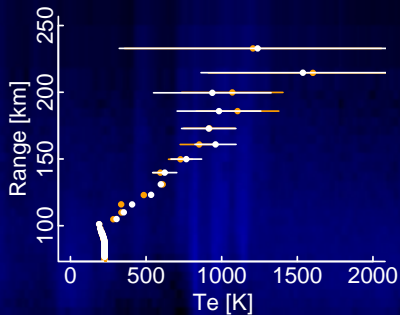
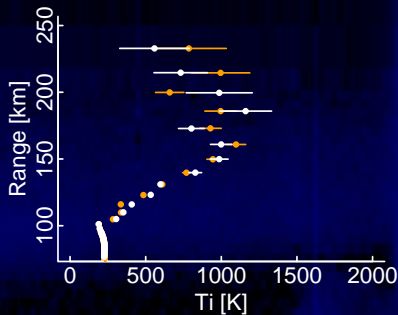
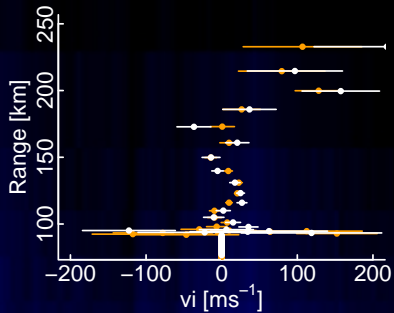
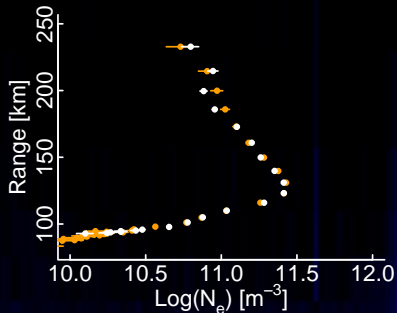
MANDA, Nov. 25th 2006, 22:05 UT, 6s integration time, real part



MANDA, Nov. 25th 2006, 22:05 UT, 6s integration time,
imaginary part



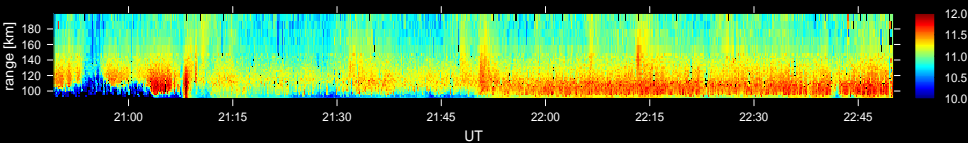
MANDA, Nov. 25th 2006, 22:05 UT, 1 min integration time



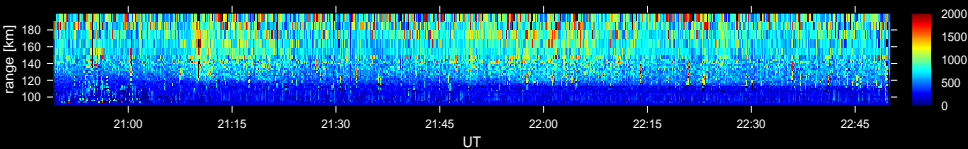
Binary code pair experiment

- ▶ Nov. 26th 2006
- ▶ 21-bit binary code pair
- ▶ Bit length $10 \mu\text{s}$
- ▶ In this example:
 - ▶ Full lags 1,2,...,17,18
 - ▶ In each full lag $\pm 2 \mu\text{s}$ fractional lags included
 - ▶ Time resolution 10 seconds
 - ▶ Range resolution 2 km

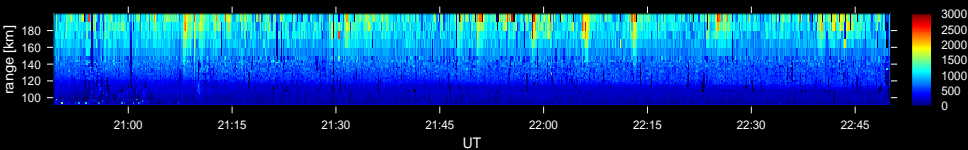
$\text{Log}(N_e) [\text{m}^{-3}]$



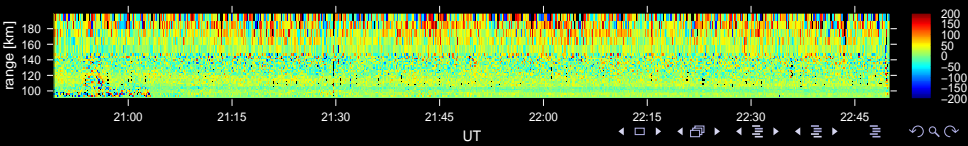
Ion Temperature [K]



Electron Temperature [K]



Ion velocity [ms^{-1}]



Summary

- ▶ Lag profile inversion was introduced as an analysis method for any phase and / or amplitude modulated ISR experiment
- ▶ Lag profile inversion was successfully used for analysing alternating code experiment
- ▶ A new experiment with a phase code pair was designed
- ▶ Amplitude data from the new experiment was successfully analysed with lag profile inversion